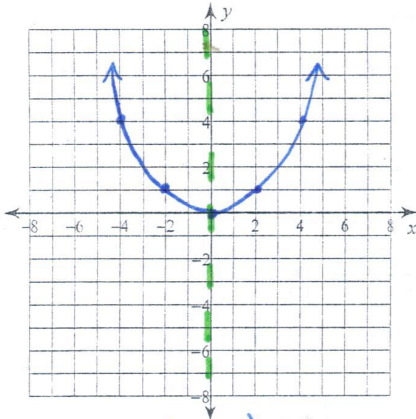


Conic Sections Review

Graph each equation and identify the following features.

1)  $y = \frac{1}{4}x^2$



Vertex:  $(0, 0)$

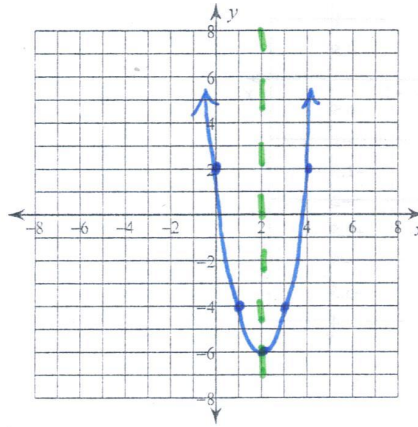
Min or Max

Axis of Symmetry:  $x = 0$

Domain:  $(-\infty, \infty)$

Range:  $[0, \infty)$

2)  $y = 2(x - 2)^2 - 6$



Vertex:  $(2, -6)$

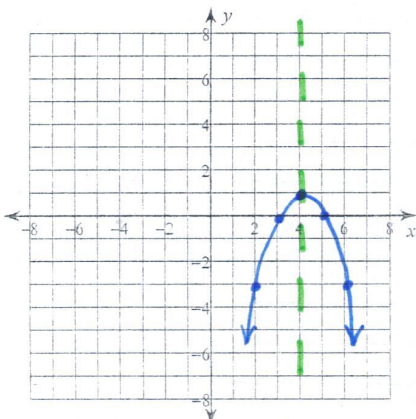
Min or Max

Axis of Symmetry:  $x = 2$

Domain:  $(-\infty, \infty)$

Range:  $[-6, \infty)$

3)  $y = -(x - 4)^2 + 1$



Vertex:  $(4, 1)$

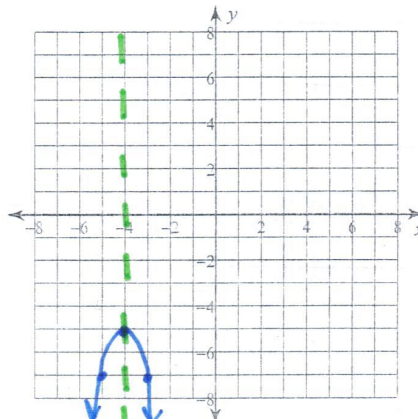
Min or Max

Axis of Symmetry:  $x = 4$

Domain:  $(-\infty, \infty)$

Range:  $(-\infty, 1]$

4)  $y = -2(x + 4)^2 - 5$



Vertex:  $(-4, -5)$

Min or Max

Axis of Symmetry:  $x = -4$

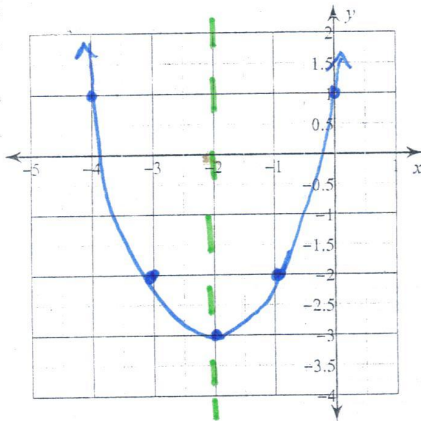
Domain:  $(-\infty, \infty)$

Range:  $(-\infty, -5]$

Sketch the graph of each function. Identify the vertex and the axis of symmetry. Then change the equation to standard form.

5)  $y = (x + 2)^2 - 3$

$x^2 + 4x + 4 - 3$



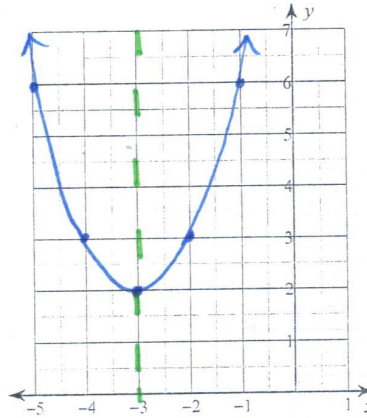
Vertex:  $(-2, -3)$

Axis of Symmetry:  $x = -2$

Standard:  $y = x^2 + 4x + 1$

6)  $y = (x + 3)^2 + 2$

$x^2 + 6x + 9 + 2$



Vertex:  $(-3, 2)$

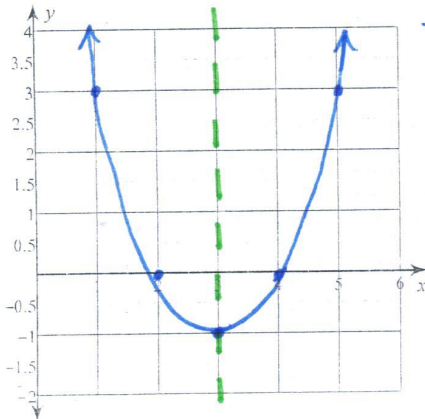
Axis of Symmetry:  $x = -3$

Standard:  $y = x^2 + 6x + 11$

Change the equation to vertex form. Sketch the graph. Identify the vertex and the axis of symmetry.

7)  $y = x^2 - 6x + 8$

$x^2 - 6x + 9 + 8 - 9$



$-\frac{b}{2} = (-3)^2$   
 $(x-3)^2 - 1$

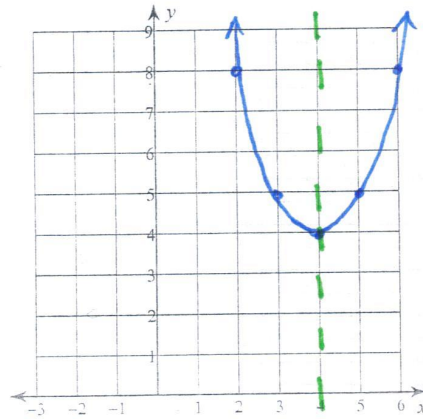
Vertex Form:  $y = (x-3)^2 - 1$

Vertex:  $(3, -1)$

Axis of Symmetry:  $x = 3$

8)  $y = x^2 - 8x + 20$

$x^2 - 8x + 16 + 20 - 16$



$-\frac{b}{2} = (-4)^2$   
 $(x-4)^2 + 4$

Vertex Form:  $y = (x-4)^2 + 4$

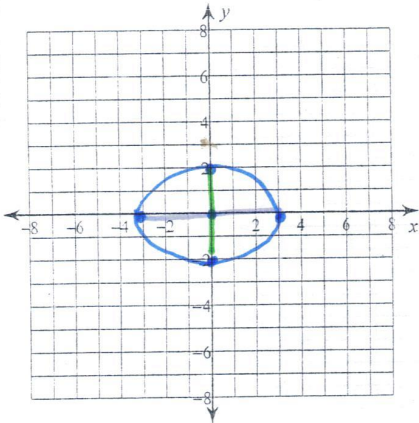
Vertex:  $(4, 4)$

Axis of Symmetry:  $x = 4$

(C) (V) (F)

Identify the center, vertices, foci, length of the major axis, and length of the minor axis of each. Then sketch the graph.

9)  $\frac{x^2}{9} + \frac{y^2}{4} = 1$



$c^2 = 9 - 4$   
 $c = \pm\sqrt{5}$

C: (0,0)

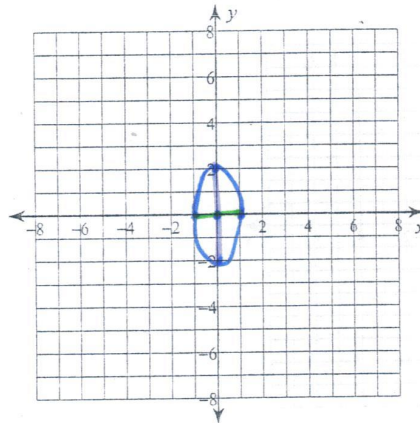
V: (-3,0)  $\neq$  (3,0)

F: (- $\sqrt{5}$ ,0)  $\neq$  ( $\sqrt{5}$ ,0)

Major: 6 units

Minor: 4 units

10)  $x^2 + \frac{y^2}{4} = 1$



$c^2 = 4 - 1$   
 $c = \pm\sqrt{3}$

C: (0,0)

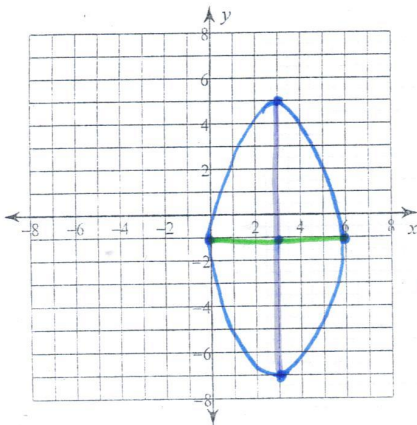
V: (0,2)  $\neq$  (0,-2)

F: (0, $\sqrt{3}$ )  $\neq$  (0,- $\sqrt{3}$ )

Major: 4 units

Minor: 2 units

11)  $\frac{(x-3)^2}{9} + \frac{(y+1)^2}{36} = 1$



$c^2 = 36 - 9$   
 $c = \pm\sqrt{27}$

C: (3,-1)

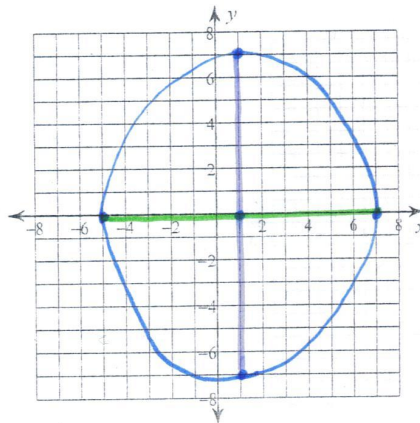
V: (3,5)  $\neq$  (3,-7)

F: (3,-1+ $\sqrt{27}$ )  $\neq$  (3,-1- $\sqrt{27}$ )

Major: 12 units

Minor: 6 units

12)  $\frac{(x-1)^2}{36} + \frac{y^2}{49} = 1$



$c^2 = 49 - 36$   
 $c = \pm\sqrt{13}$

C: (1,0)

V: (1,7)  $\neq$  (1,-7)

F: (1, $\sqrt{13}$ )  $\neq$  (1,- $\sqrt{13}$ )

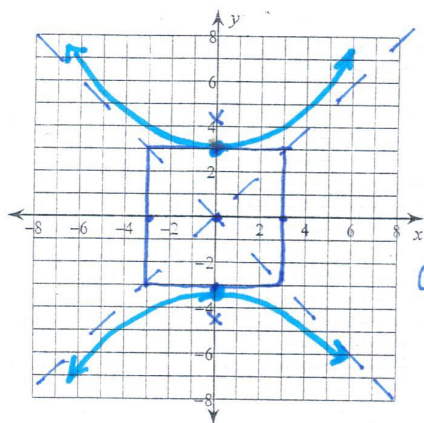
Major: 14 units

Minor: 12 units



Identify the vertices, foci, length of the transverse axis, and length of the conjugate axis of each. Then sketch the graph.

13)  $\frac{y^2}{9} - \frac{x^2}{9} = 1$   $C = (0,0)$



opens upward & downward

$c^2 = 9+9$   
 $c = \pm\sqrt{18}$

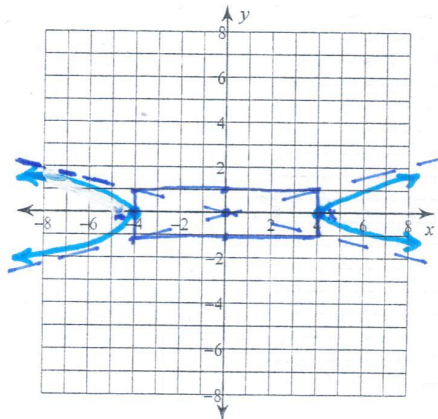
V:  $(0,3) \neq (0,-3)$

F:  $(0,\sqrt{18}) \neq (0,-\sqrt{18})$

TA: 6 units

CA: 6 units

14)  $\frac{x^2}{16} - y^2 = 1$   $C = (0,0)$



opens L/R

TA =  $2a = 2(4)$   
CA =  $2b = 2(1)$

$c^2 = 16+1$   
 $c = \pm\sqrt{17}$

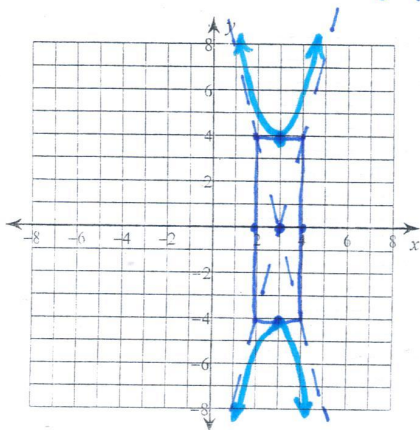
V:  $(-4,0) \neq (4,0)$

F:  $(\sqrt{17},0) \neq (-\sqrt{17},0)$

TA: 8 units

CA: 2 units

15)  $\frac{y^2}{16} - (x-3)^2 = 1$   $C = (3,0)$



opens up/down

$c^2 = 16+1$   
 $c = \pm\sqrt{17}$

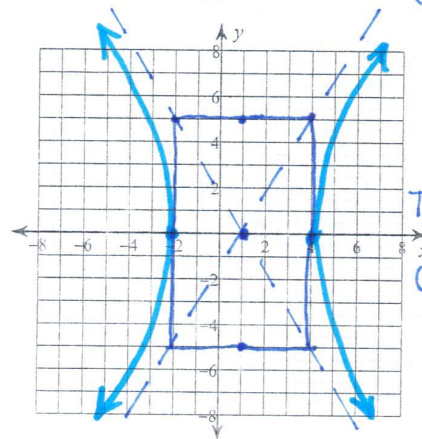
V:  $(3,4) \neq (3,-4)$

F:  $(3,\sqrt{17}) \neq (3,-\sqrt{17})$

TA: 8 units

CA: 2 units

16)  $\frac{(x-1)^2}{9} - \frac{y^2}{25} = 1$   $C = (1,0)$



opens L/R

TA =  $2a = 2(3)$   
CA =  $2b = 2(5)$

$c^2 = 9+25$   
 $c = \pm\sqrt{34}$

V:  $(4,0) \neq (-2,0)$

F:  $(1+\sqrt{34},0) \neq (1-\sqrt{34},0)$

TA: 6 units

CA: 10 units

Write the equation of the parabola with vertex at the origin and the given focus.

17) Focus at  $(0, 2)$

$c=2$   $a = \frac{1}{4c} = \frac{1}{4(2)} = \frac{1}{8}$

$y = \frac{1}{8}x^2$

18) Focus at  $(4, 0)$

$c=4$   $a = \frac{1}{4(4)} = \frac{1}{16}$

$x = \frac{1}{16}y^2$

19) Focus at  $(-8, 0)$

$c=-8$   $a = \frac{1}{4(-8)} = -\frac{1}{32}$

$x = -\frac{1}{32}y^2$

Write the equation of the parabola with vertex at the origin and the given directrix.

20) Directrix  $y=2$

$c=-2$   $a = -\frac{1}{8}$

$y = -\frac{1}{8}x^2$

21) Directrix  $x=-6$

$c=6$   $a = \frac{1}{4(6)} = \frac{1}{24}$

$x = \frac{1}{24}y^2$

Write the equation of the parabola with the given vertex and focus.

22) Vertex  $(1, 2)$ ; Focus  $(-1, 2)$

$c=-2$   $a = -\frac{1}{8}$

$x = -\frac{1}{8}(y-2)^2 + 1$

23) Vertex  $(2, 5)$ ; Focus  $(2, 6)$

$c=1$   $a = \frac{1}{4}$

$y = \frac{1}{4}(x-2)^2 + 5$

Find the vertex, focus, and directrix of each parabola.

24)  $y = \frac{1}{20}x^2$

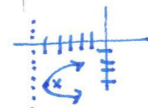
$a = \frac{1}{20}$   $c = \left| \frac{1}{4a} \right| = \left| \frac{1}{4(\frac{1}{20})} \right| = 5$

Vertex:  $(0, 0)$   
focus:  $(0, 5)$   
directrix:  $y = -5$

25)  $x = y^2 - 8y + 11$

$x = y^2 - 8y + 16 + 11 - 16$   
 $-\frac{8}{2} = -4$   $x = (y-4)^2 - 5$

vertex:  $(-5, 4)$   
focus:  $(-4.75, 4)$



$a=1$   $c = \left| \frac{1}{4a} \right| = \frac{1}{4} = 0.25$

directrix:  $x = -5.25$

Find the center and radius of each circle.

26)  $(x-3)^2 + (y-4)^2 = 4$

center: (3, 4)

radius: 2

27)  $x^2 + (y+8)^2 = 49$

center: (0, -8)

radius: 7

28)  $(x+4)^2 + y^2 = 8$

center: (-4, 0)

radius:  $\sqrt{8}$  or  $2\sqrt{2}$

Use the given information to write the equation of the circle.

29) Radius: 4

Center: (1, 3)

$$(x-1)^2 + (y-3)^2 = 16$$

30) Radius: 1

Center: (-1, 5)

$$(x+1)^2 + (y-5)^2 = 1$$

31) Center: (1, -2)

Area:  $4\pi$

$$\downarrow$$

$$\pi r^2$$

$$\pi r^2 = 4\pi$$

$$r = 2$$

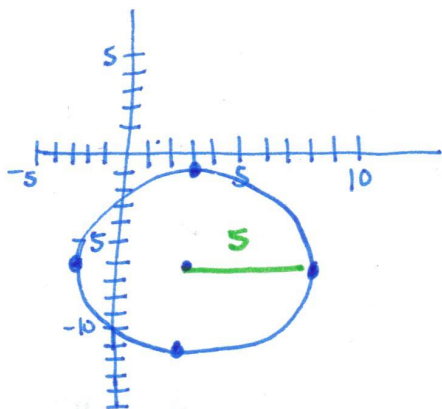
$$(x-1)^2 + (y+2)^2 = 4$$

Sketch the graph of the circle.

32)  $(x-3)^2 + (y+6)^2 = 25$

center:  
(3, -6)

radius: 5



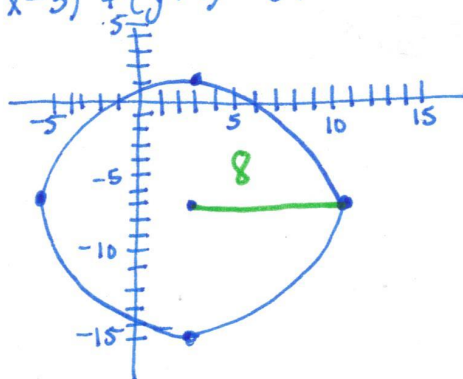
33)  $x^2 + y^2 - 6x + 14y = 6$

$$x^2 - 6x + 9 + y^2 + 14y + 49 = 6 + 9 + 49$$

$$\frac{-6}{2} = (-3)^2 \quad \frac{+14}{2} = (+7)^2$$

$$(x-3)^2 + (y+7)^2 = 64$$

center:  
(3, -7)  
radius: 8





Review of Previous Material

Solve each equation by taking square roots.

$$1) 3a^2 + 4 = -8$$

$$\frac{-4 \quad -4}{3a^2 = -12}$$

$$\frac{3a^2 = -12}{3} \quad \frac{-12}{3}$$

$$\sqrt{a^2} = \sqrt{-4} \quad \boxed{a = \pm 2i}$$

$$2) 6x^2 - 5 = -37$$

$$\frac{+5 \quad +5}{6x^2 = -32}$$

$$\frac{-32}{6}$$

$$\sqrt{x^2} = \sqrt{\frac{-16}{3}}$$

$$\boxed{x = \frac{\pm 4i}{\sqrt{3}}}$$

Solve each equation by factoring.

$$3) v^2 - 8v + 12 = 0$$

$$(v-6)(v-2) = 0$$

$$\boxed{v = 6, 2}$$

$$4) n^2 - 2n - 15 = 0$$

$$(n-5)(n+3) = 0$$

$$\boxed{n = 5, -3}$$

Solve each equation by completing the square.

$$5) a^2 + 2a - 41 = 7$$

$$a^2 + 2a + \underline{1} = 48 + \underline{1}$$

$$\frac{+2}{2} = (+1)^2$$

$$\sqrt{(a+1)^2} = \sqrt{49}$$

$$a+1 = \pm 7$$

$$\begin{matrix} a = 7-1 = 6 \\ a = -7-1 = -8 \end{matrix} \quad \boxed{\begin{matrix} 6 \\ -8 \end{matrix}}$$

$$6) p^2 - 14p + 20 = -9$$

$$p^2 - 14p + \underline{49} = -29 + \underline{49}$$

$$\frac{-14}{2} = (-7)^2$$

$$\sqrt{(p-7)^2} = \sqrt{20}$$

$$p-7 = \pm\sqrt{20}$$

$$\boxed{p = 7 \pm \sqrt{20}}$$

Find the discriminant of each quadratic equation then state the number and type of solutions.

$$7) -7a^2 - a - 4 = 0 \rightarrow b^2 - 4ac$$

$$\begin{matrix} a = -7 \\ b = -1 \\ c = -4 \end{matrix}$$

$$(-1)^2 - 4(-7)(-4)$$

$$1 - 112 = -111$$

$$\boxed{\therefore 2 \text{ imaginary roots}}$$

$$8) 3n^2 - 6n + 3 = 0$$

$$\begin{matrix} a = 3 \\ b = -6 \\ c = 3 \end{matrix}$$

$$(-6)^2 - 4(3)(3)$$

$$36 - 36 = 0$$

$$\boxed{\therefore 1 \text{ Real Root}}$$

Solve each equation with the quadratic formula.

$$9) 4b^2 + 2b - 42 = 0$$

$$\begin{matrix} a = 4 \\ b = 2 \\ c = -42 \end{matrix}$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(4)(-42)}}{2(4)}$$

$$4 + 672$$

$$x = \frac{-2 \pm \sqrt{676}}{8} = \frac{-2 \pm 26}{8}$$

$$\begin{matrix} \frac{-2+26}{8} = 3 \\ \frac{-2-26}{8} = -\frac{7}{2} \end{matrix} \quad \boxed{\begin{matrix} 3 \\ -\frac{7}{2} \end{matrix}}$$

$$10) 5a^2 + 2a - 51 = 0$$

$$\begin{matrix} a = 5 \\ b = 2 \\ c = -51 \end{matrix}$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(5)(-51)}}{2(5)}$$

$$4 + 1020$$

$$x = \frac{-2 \pm \sqrt{1024}}{10} = \frac{-2 \pm 32}{10}$$

$$\begin{matrix} \frac{-2+32}{10} = 3 \\ \frac{-2-32}{10} = -\frac{17}{5} \end{matrix} \quad \boxed{\begin{matrix} 3 \\ -\frac{17}{5} \end{matrix}}$$