

## Section 14-5 Notes

### Probability Models

For Exercises 1-3, use the two-way frequency table below. It shows the number of pets owned by classmates and whether or not the pets live outside.

	Lives outside	Live inside	Totals
Dogs	17	7	24
Cats	8	8	16
Totals	25	15	40

1. What is the probability that a randomly chosen animal is a cat that lives outside?

Set up a fraction using the number of cats that live outside as the numerator, and the total animal population as the denominator. Then simplify.  $\frac{8}{40} = \frac{1}{5}$

*"given" only look at the data in that row or column*

2. What is  $P(\text{is a dog} \mid \text{lives outside})$ ? *\* Only look at the "lives outside" column.*

Set up a fraction using the number of dogs that live outside as the numerator, and the total number of animals who live outside as the denominator. Then simplify.  $\frac{17}{25} = \frac{17}{25}$

3. What is  $P(\text{lives outside} \mid \text{is a dog})$ ?  $= \frac{17}{24}$  *\* Only look at the "Dogs" row.*

For Exercises 4-7, use the two-way frequency table below. It shows the swimming preference of 100 men and women who visited a lakeside resort.

	Pool	Lake	Totals
Men	18	25	43
Women	22	35	57
Totals	40	60	100

4. What is the probability that a randomly chosen person is a man who prefers the pool?  $\frac{18}{100} = \frac{9}{50}$

5. What is the probability that a randomly chosen person is a woman given that the person prefers the pool?  $P(\text{woman} \mid \text{pool}) = \frac{22}{40} = \frac{11}{20}$  *\* Only look at the "Pool" column.*

6. What is the probability that a randomly chosen person prefers the lake, given that the person is a man?  $P(\text{lake} \mid \text{man}) = \frac{25}{43}$  *\* Only look at the "Men" row.*

**Practice** (continued)

Form K

Probability Models

For Exercises 7–9, use the two-way frequency table below. It shows where some students prefer to study.

	Library	Home	Cafe	Totals
Freshman	1	8	1	10
Sophomore	3	4	3	10
Totals	4	12	4	20

7. What is the probability that a randomly chosen student is a freshman given that the student prefers to study at home?

*only "home" column*  
 $P(F | \text{Home}) = \frac{8}{12} = \boxed{\frac{2}{3}}$

8. What is  $P(\text{prefers the library} | \text{is a sophomore})$ ?

*only "Soph" row.*  
 $= \boxed{\frac{3}{10}}$

9. Reasoning Explain why the bottom row and the far-right column of the table have the same sum.

*so you can know the total for each row/column to use in the probabilities.*

The table below is a relative frequency distribution for people who are interested in building rowboats. Use the table for Exercises 10 and 11.

	Watched the video	Did not watch the video	Totals
Built a rowboat	0.5	0.1	0.6
Did not build a row boat	0.3	0.1	0.4
Totals	0.8	0.2	1

10. What is the probability that a person who watched the video built a rowboat?

*only use "watched" column.*  
 $P(\text{rowboat} | \text{watched video}) = \frac{0.5}{0.8} = \boxed{\frac{5}{8}}$   
 or 0.625

To start, set up a fraction with the relative frequency of people that watched the video as the denominator:  $\frac{\quad}{0.8} = \frac{\quad}{\quad}$

11. What is  $P(\text{built a rowboat} | \text{didn't watch the video})$ ?

*only "didn't watch" column.*  
 $= \frac{0.1}{0.2} = \boxed{\frac{1}{2} \text{ or } .5}$